

CENTRE DE RECHERCHE ASTROPHYSIQUE DE LYON

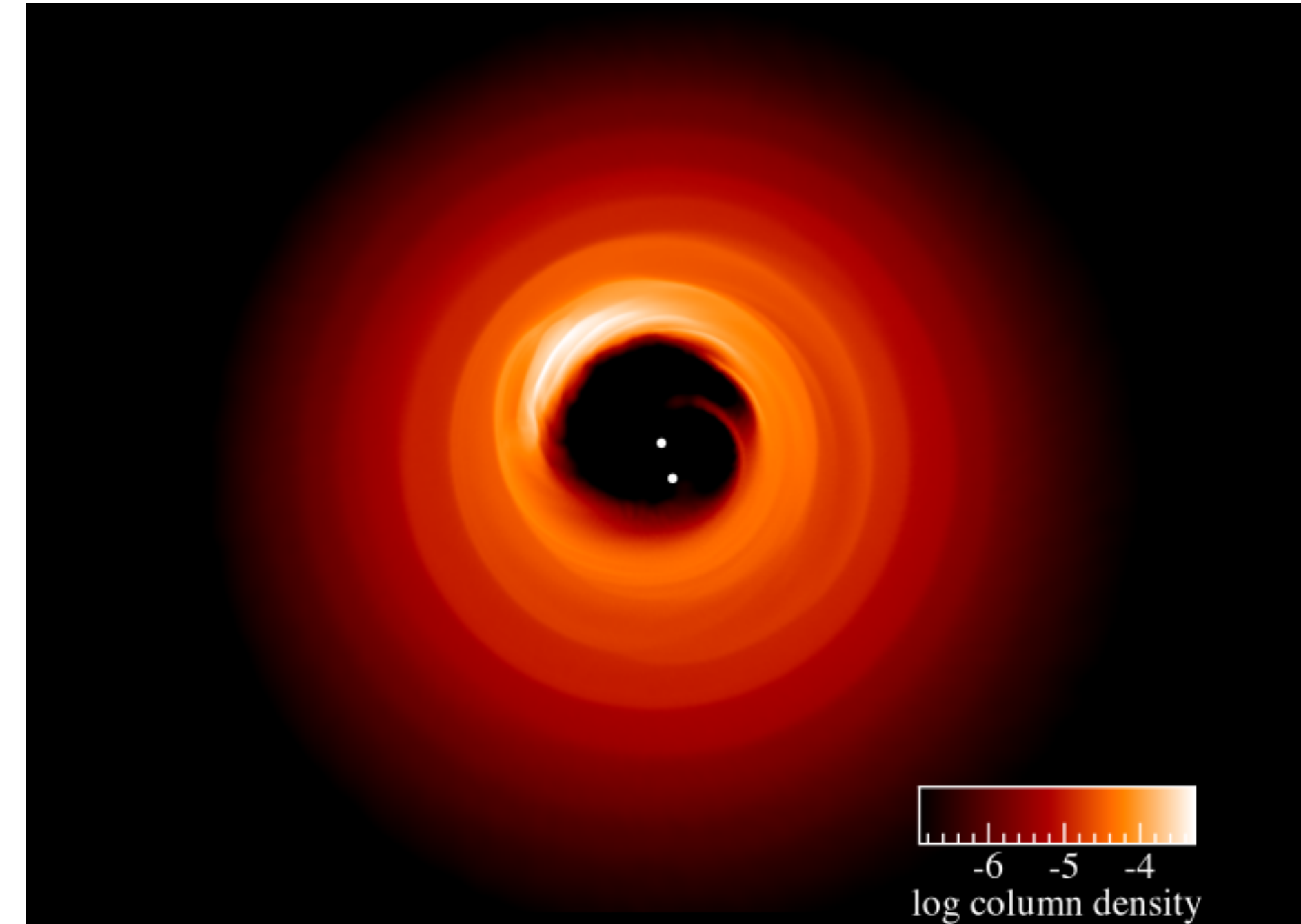


## WHY ECCENTRIC DISCS?

- Numerous possible causes for eccentric discs:
  - Binaries and planets (e.g. Ragusa et al. 2020)
  - Flybys (e.g. Cuello et al. 2020)
  - Non-spherical collapse
- Interest beyond protostellar discs:
  - Eccentric debris discs (Olofsson et al. 2019)
  - Discs around white dwarfs (e.g. Manser et al. 2014)
  - Tidal disruption events (e.g. Bonnerot et al. 2016)
  - X-ray binaries (e.g. Lubow 1991)
- Key to understand dissipation in accretion discs:
  - Turbulence  $\neq$  viscosity
  - Why discs are so damn circular then?!

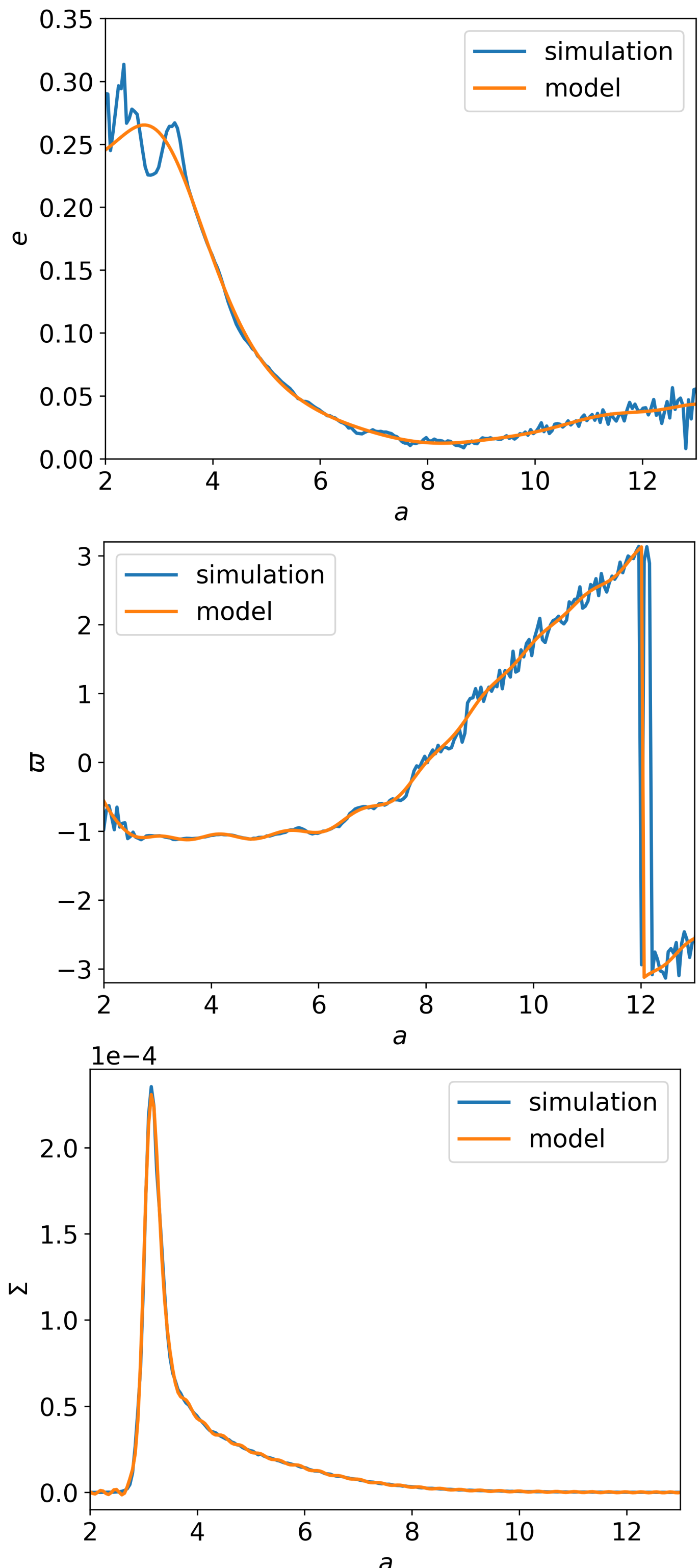
## PROOF OF PERFORMANCE

We compare the dynamics of a 3D SPH numerical simulation (PHANTOM, Price et al. 2018) of an eccentric circumbinary with the model.



## ANALYTICAL MODEL

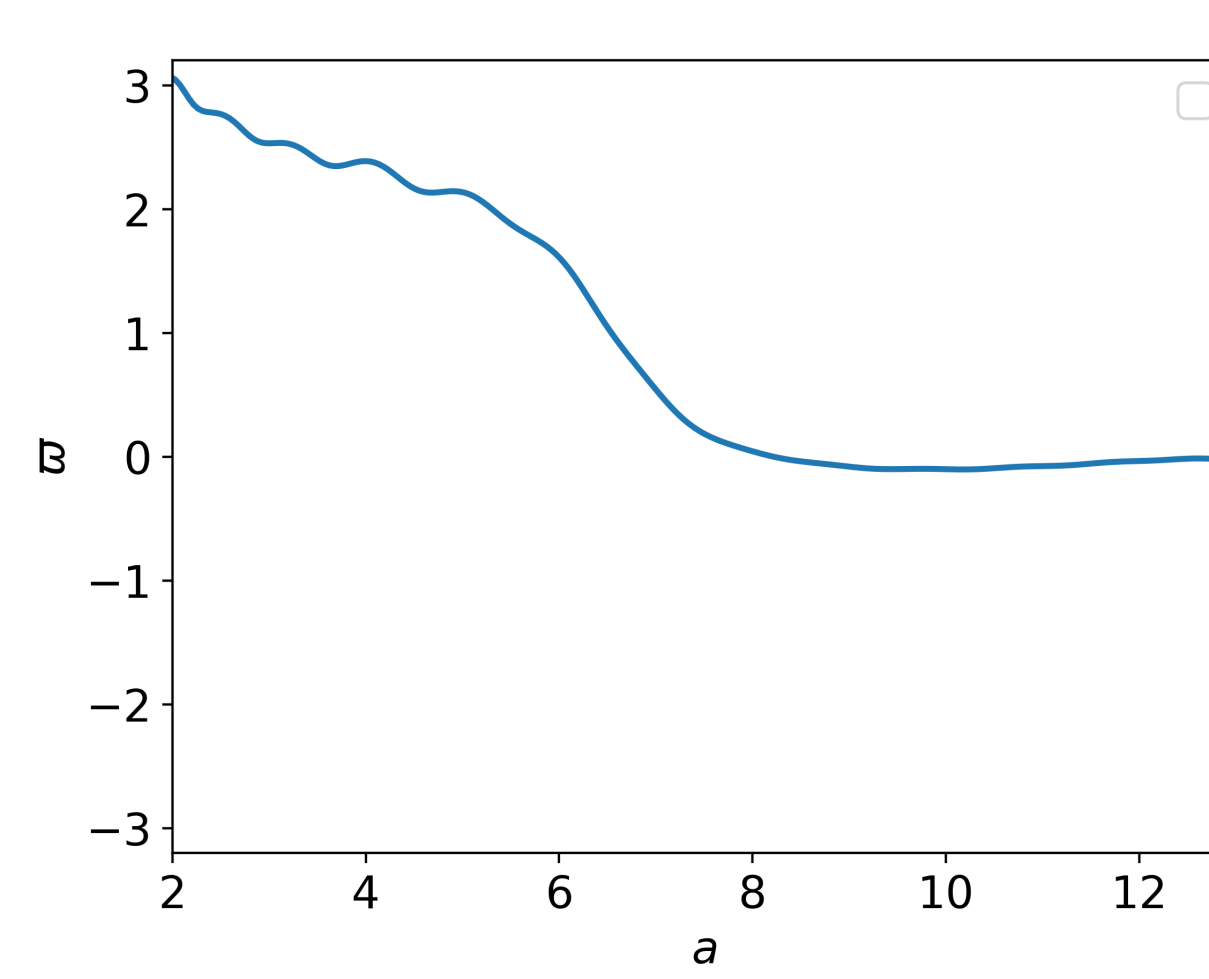
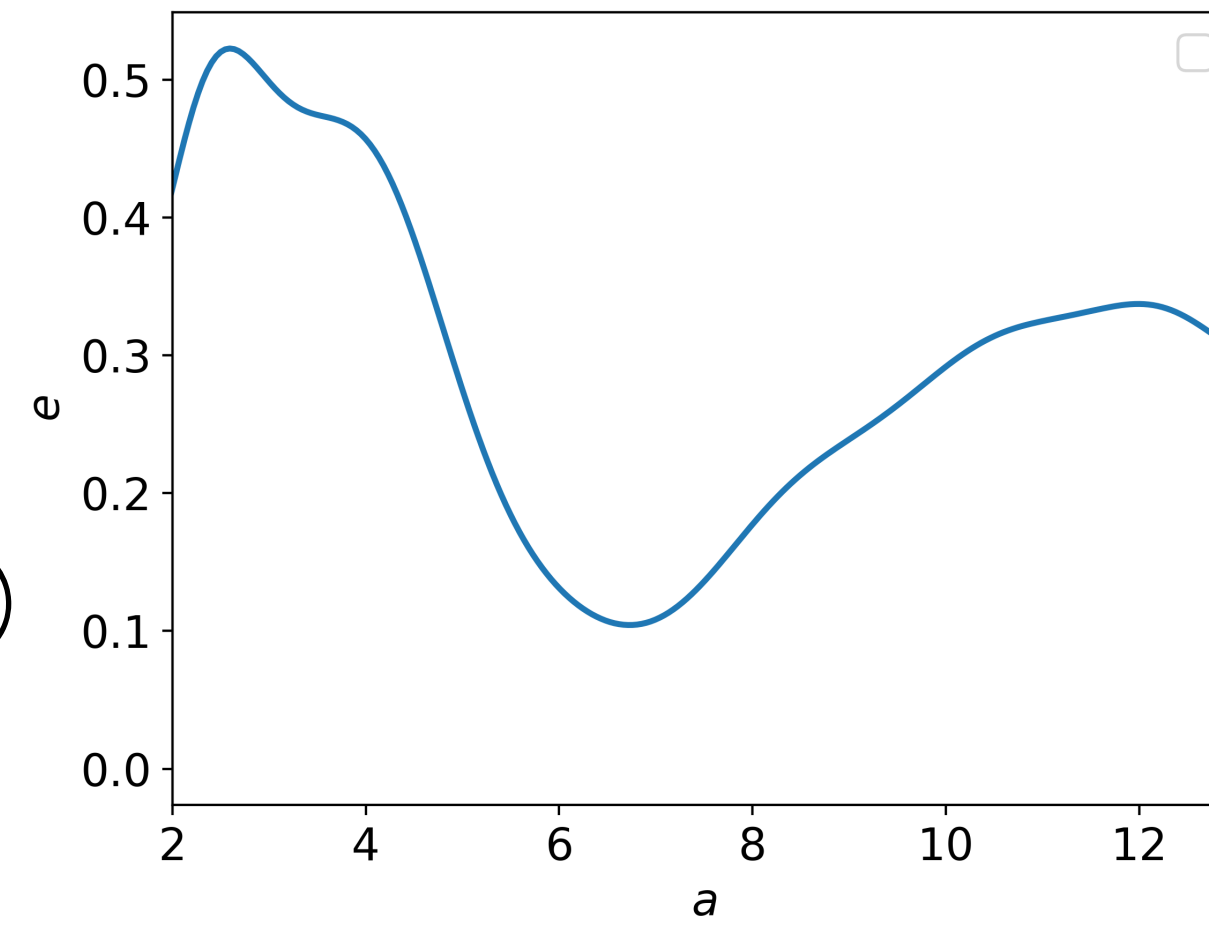
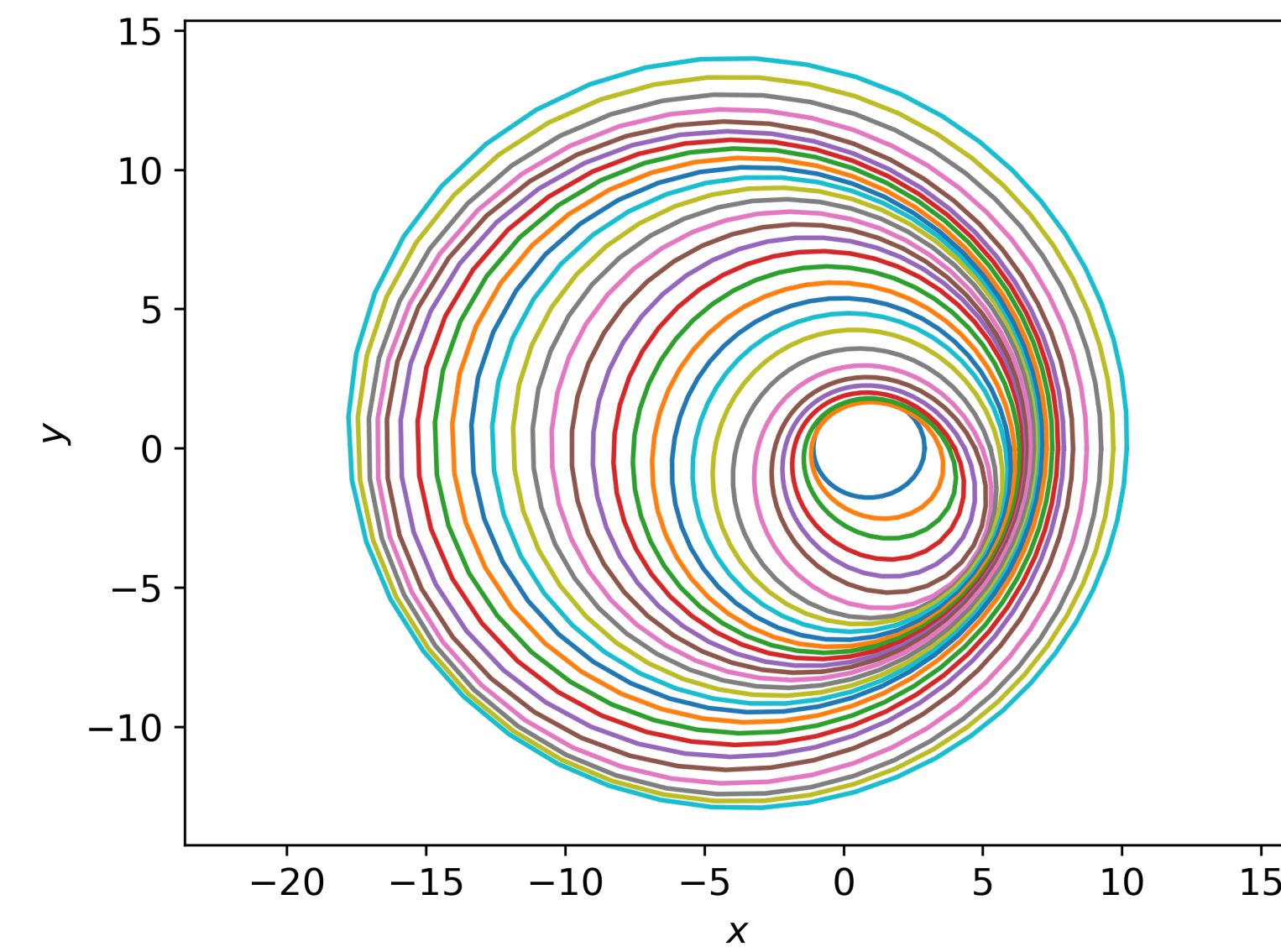
We create an analytical model from the values  $e(a)$ ,  $\varpi(a)$ ,  $\Sigma(a)$  extracted from the simulation



## HOW TO MODEL THEM? ECCENTRIC KEPLERIAN DISCS

- Set of multiple Keplerian nested ellipses
  - For fixed semi-major axis:
    - $e(a)$
    - $\varpi(a)$
- Most used formalism (e.g. Ogilvie 2001)

$$E(a) = e(a)e^{i\varpi}$$



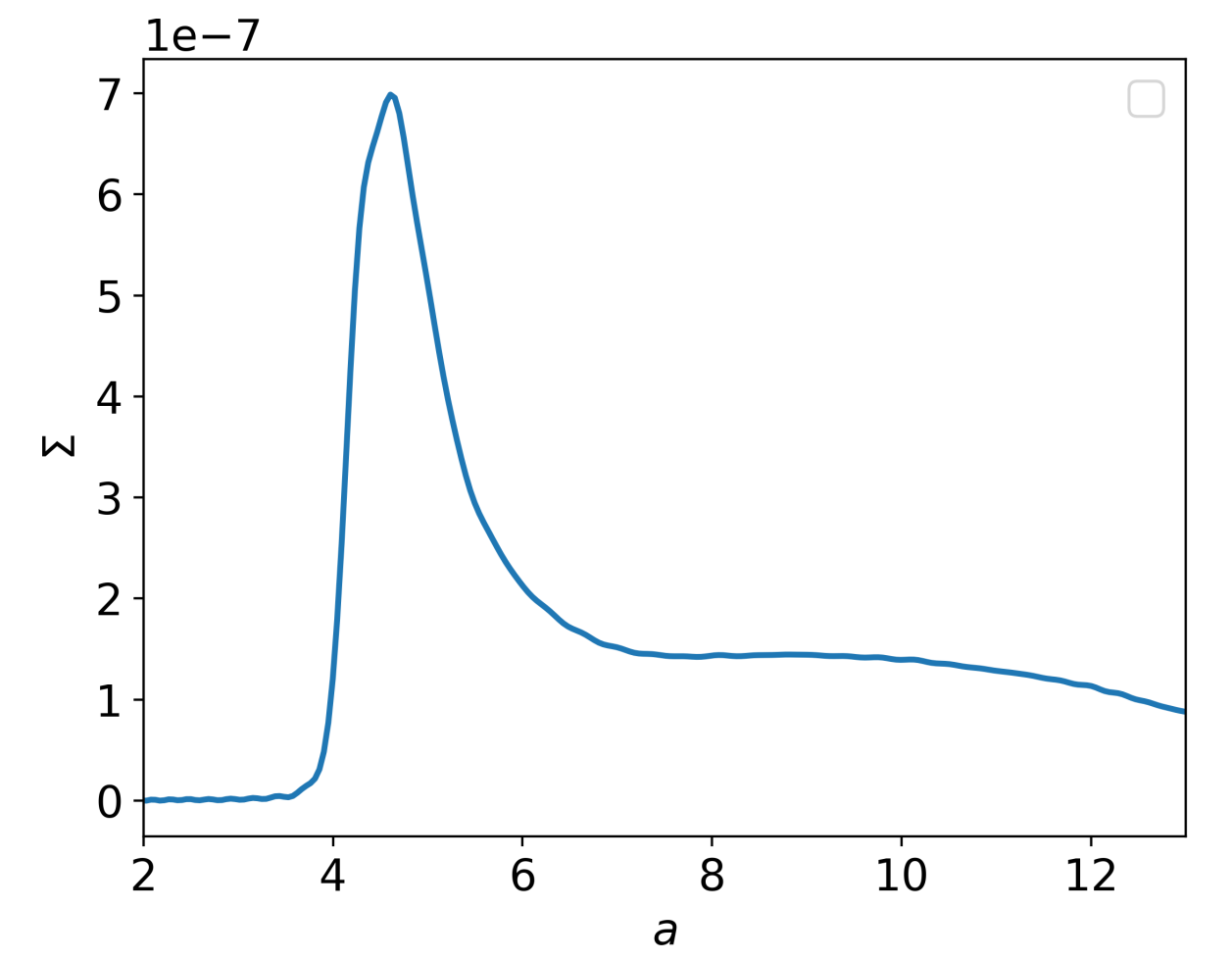
## PRESSURE EFFECTS

The negative pressure gradient makes the disc sub-keplerian. We find that a reasonable approximation is:

$$v_{\phi, \text{press}} = v_{k, \phi} + \delta v_{\phi, P}$$

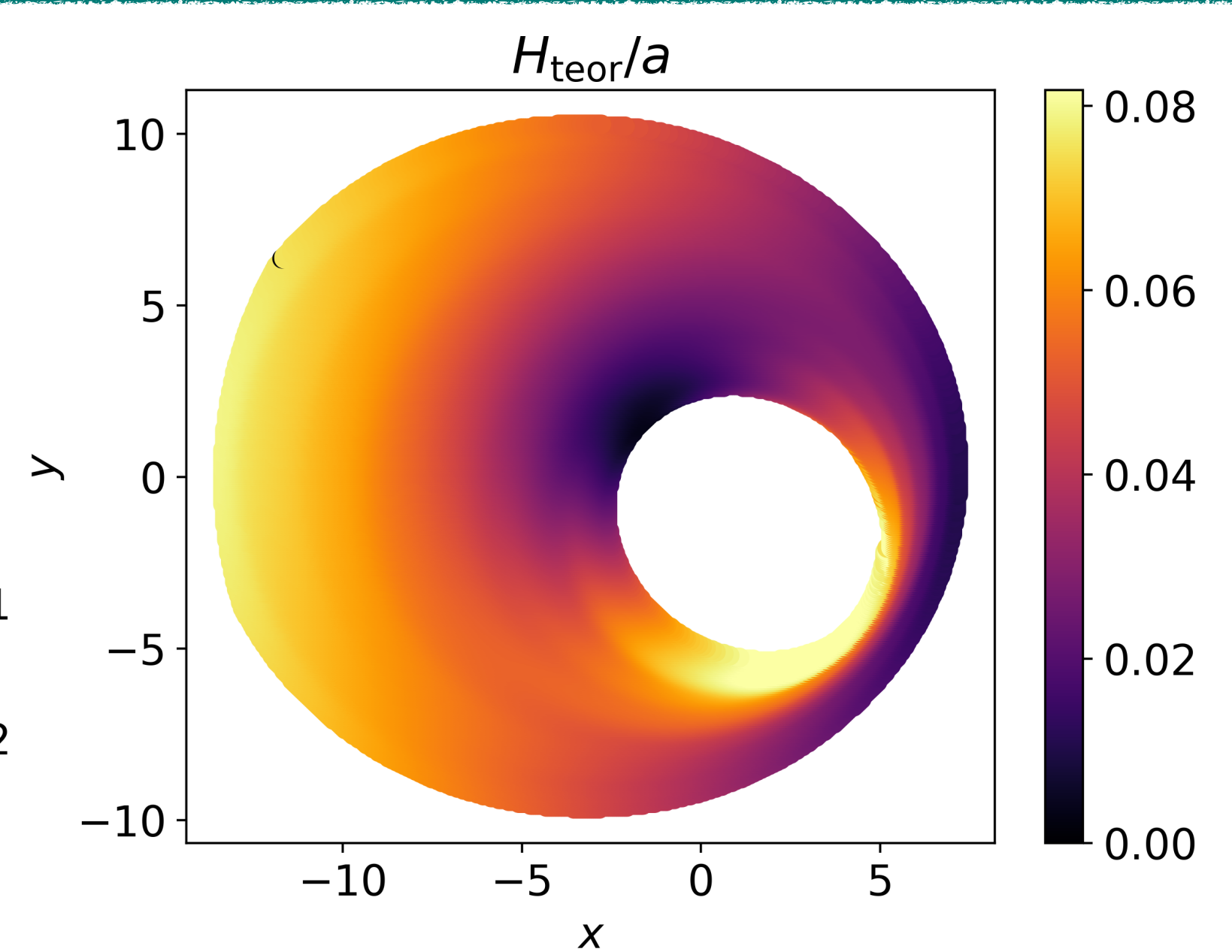
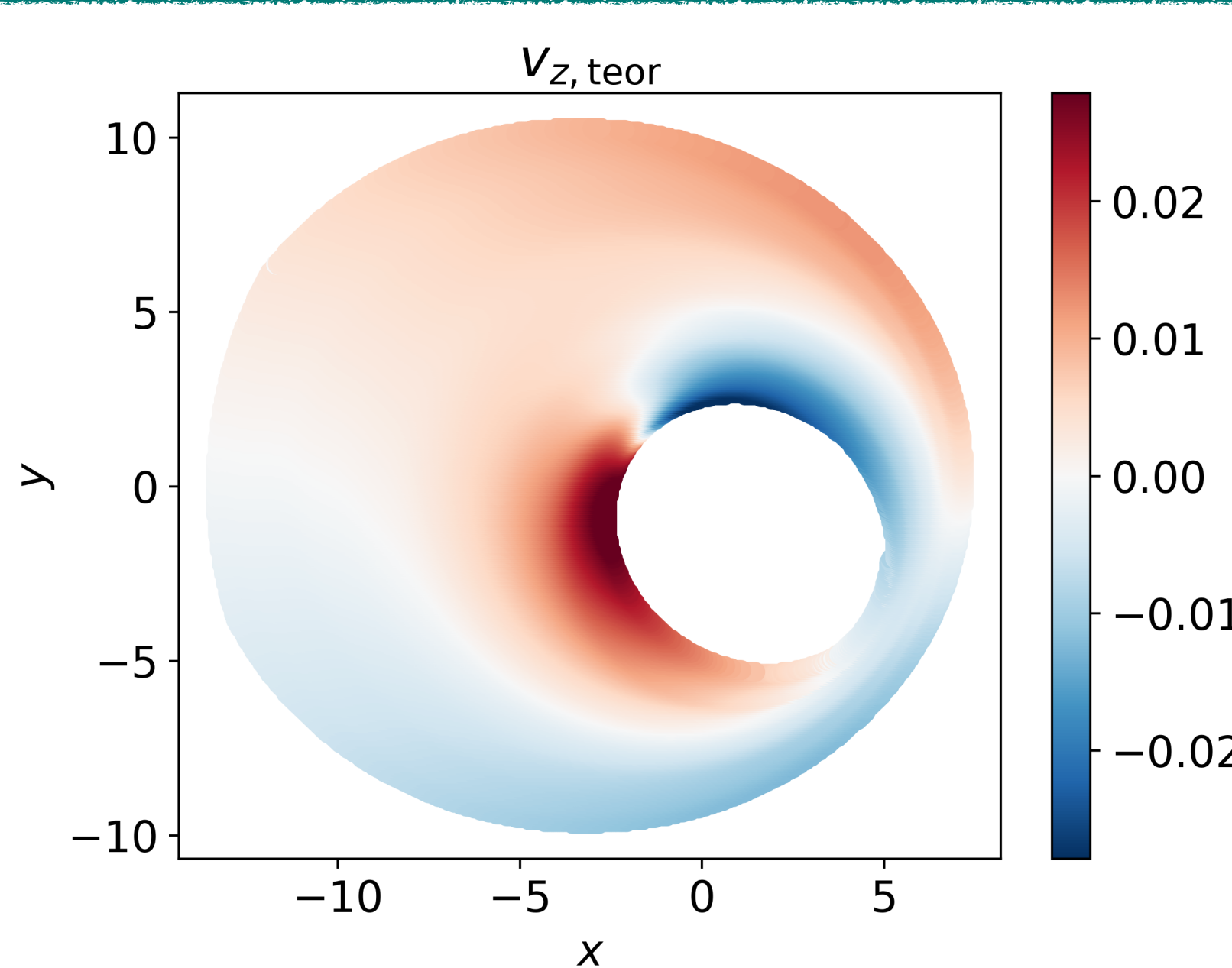
$$\delta v_{\phi, P} = -\frac{a}{\Sigma} \frac{dP}{da}$$

$$P = c_s^2 \Sigma$$

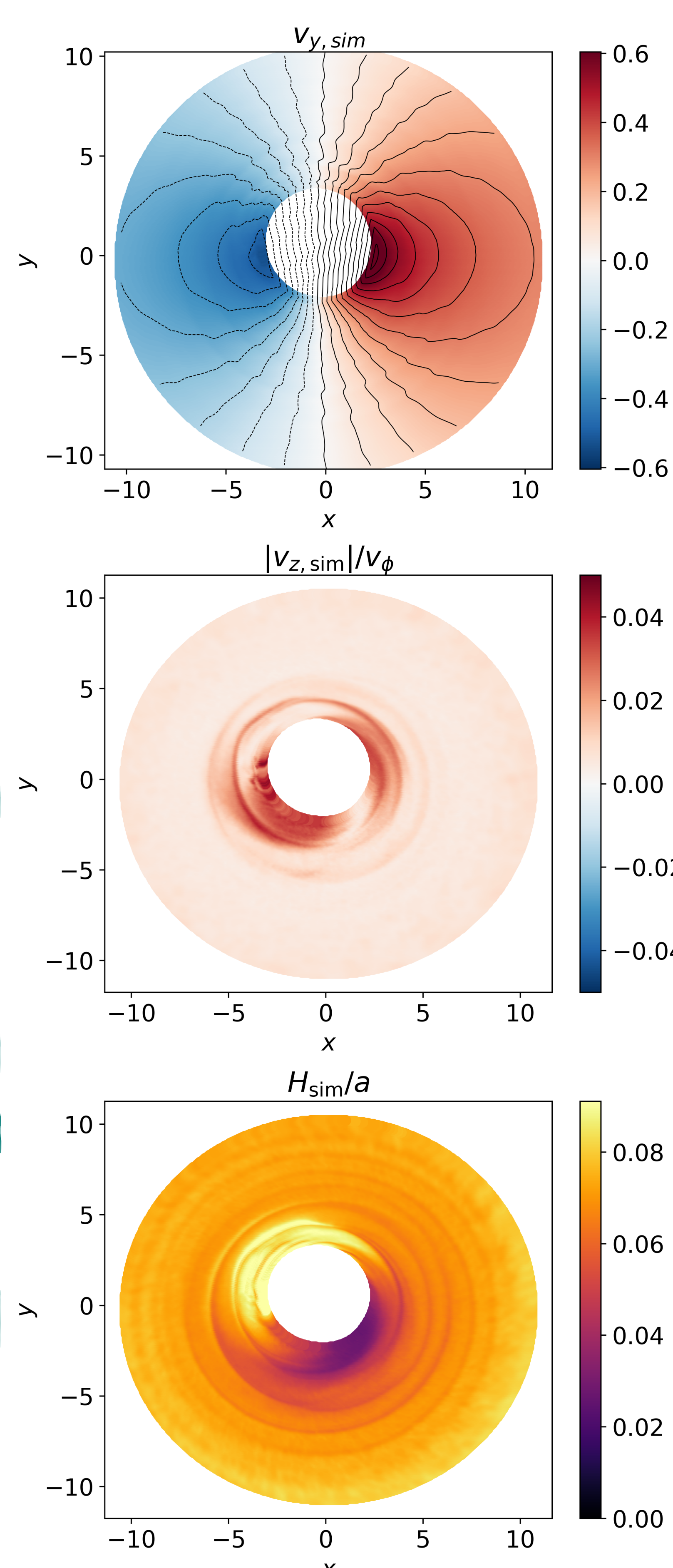


## VERTICAL MOTION

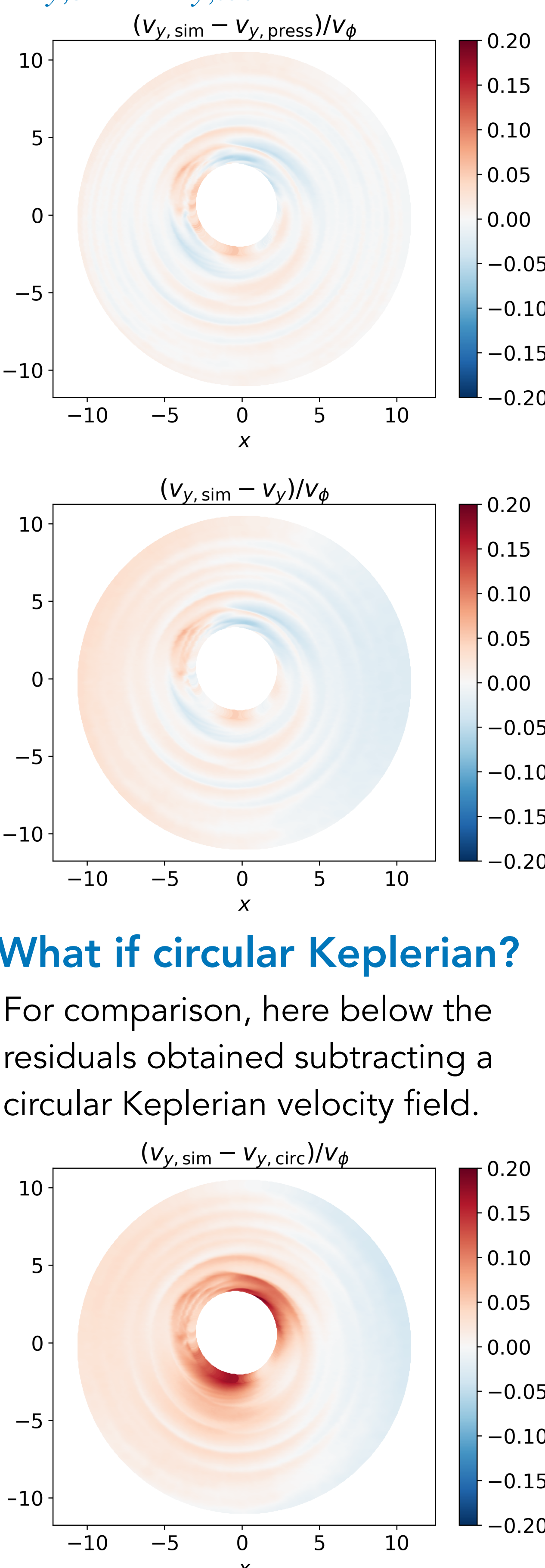
Orbit compression at pericentre and apocentre introduces vertical motion along the orbit



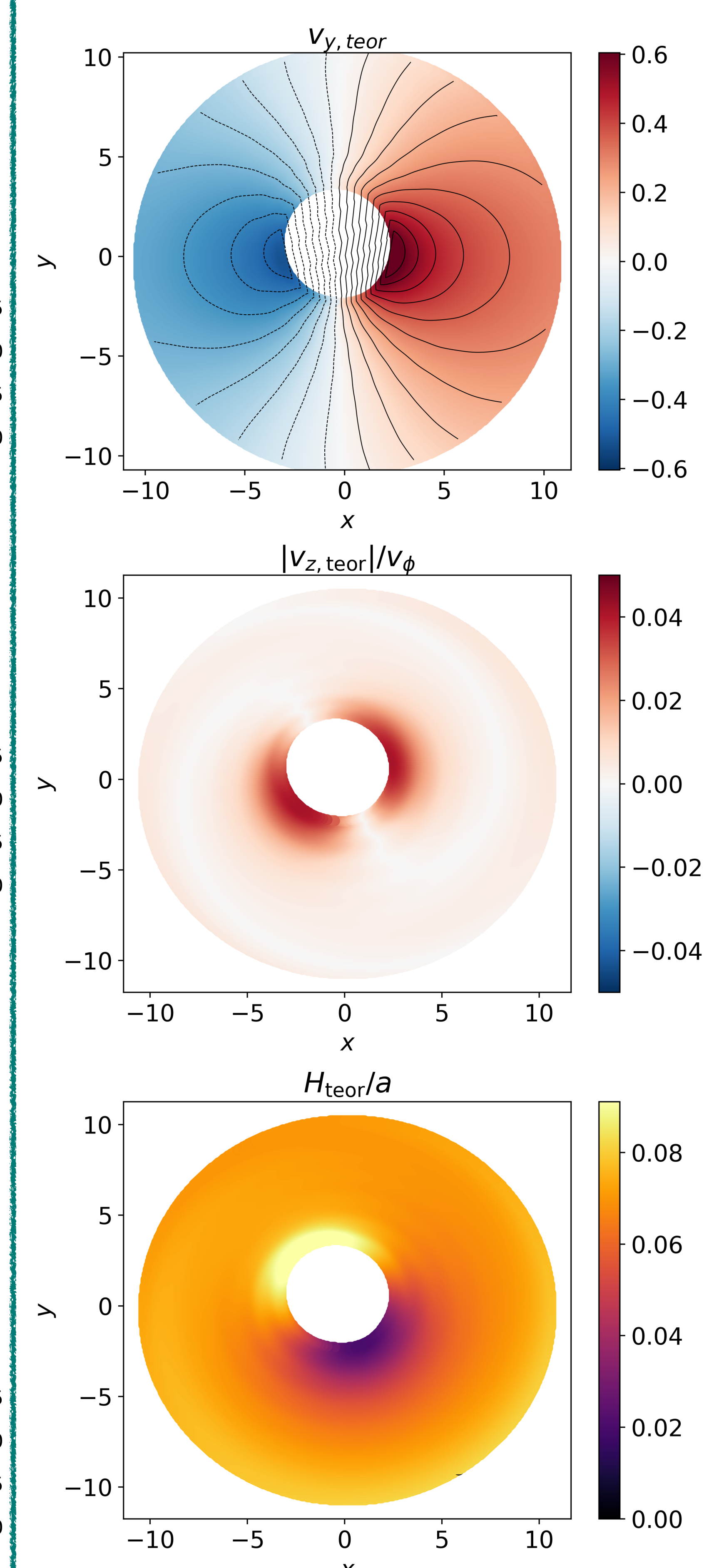
## SIMULATION



## RESIDUALS



## ANALYTICAL MODEL



## What if circular Keplerian?

For comparison, here below the residuals obtained subtracting a circular Keplerian velocity field.

References:  
 Bonnerot, C., et al. (2016), MNRAS, 455, 2253  
 Cuello, N., et al. (2020), MNRAS, 491, 504  
 Lubow, S. (1991), ApJ, 401, 317  
 Manser, C. J., et al. (2016), MNRAS, 455, 4467  
 Ogilvie, G. (2001), MNRAS, 325, 231  
 Ogilvie, G. & Barker, A. (2014), MNRAS, 445, 2621  
 Ogilvie, G. & Lynch, E. (2019), MNRAS, 483, 4453  
 Olofsson J., et al., 2019, A&A, 630, A142  
 Ragusa, E., et al. (2020), MNRAS, 499, 3362

HYDRO CODE  
 PHANTOM, 3D SPH  
 Price et al. (2018), PASA, 35, 31

